

# Equations for Robot Winch Power Assignment

## Gear Ratio

$GR = \tau_{out} / \tau_{in} = N_{out} / N_{in} = \omega_{in} / \omega_{out}$  where:  $\tau$  = torque,  $N$  = # of teeth,  $\omega$  = angular velocity ("speed")  
Note: Motor is input and gearbox is output

## Force / Work / Energy / Power

$\tau = F \cdot r$  where:  $F$  = force,  $r$  = radius

$W = Fd$  where:  $W$  = work,  $F$  = force,  $d$  = distance

$P = W/t$  (mech. power)

where:  $W$  = work,  $t$  = time

*Note: you don't have  $d$  or  $t$  in this project, so use the next equation instead.  
It is a completely equivalent equation – for a free thrill, see if you can prove it.*

$P = \tau \cdot \omega$  (mech. power)

where:  $P$  = power,  $\tau$  = torque,  $\omega$  = angular velocity ("speed")

*Note: to get  $P$  in Watts, put  $\omega$  in radians/sec, and put  $\tau$  in Nm*

*Note: 1 revolution =  $2\pi$  radians*

## Motor Equations: requires motor specification data

$\% \text{ Torque} = \% \tau = \tau / \tau_s$

where:  $\% \text{ Torque}$  = percent of max torque being used,

$T$  = actual torque,  $T_s$  = stall torque of the motor

$\omega = (1 - \% \tau) \omega_f$

where:  $\% \tau$  =  $\% \text{max Torque}$ ,  $\omega$  = speed,  $\omega_f$  = free speed of motor

$I = I_f + (I_s - I_f) \% \tau$

where:  $I$  = actual current,  $I_s$  = stall current of motor,

$I_f$  = free current of motor,  $\% \tau$  =  $\% \text{ of max torque}$

## Electrical Power / Efficiency

$V = IR$

where:  $V$  = voltage,  $I$  = current,  $R$  = resistance

$P = IV$  (elec. power)

where:  $P$  = elec. power,  $I$  = current,  $V$  = voltage

$Eff = P_{out} / P_{in}$

where:  $Eff$  = power efficiency of system,  $P_{out}$  = output power,

$P_{in}$  = input power

*Note: figure out which is input power and which is output power: mech vs elec*